

Dual polarimetric Radar Vegetation Index for Crop Growth Monitoring Using Sentinel-1 SAR Data

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Abstract

Sentinel-1 Synthetic Aperture Radar (SAR) data has provided an unprecedented opportunity for crop monitoring due to its high revisit frequency and wide spatial coverage. The dual-pol Sentinel-1 SAR data is being utilized for the European Common Agricultural Policy (CAP) as well as for other national projects, which aim to provide Sentinel derived information to support crop monitoring networks. Among the several earth observation products identified for agriculture monitoring, the vegetation status indicator is one of the critical elements that require minimum end-user expertise. In literature, several experiments usually utilize the backscatter intensities to characterize crops. In this work, we jointly use both the scattered and received wave information to derive a new vegetation index (DpRVI) for Sentinel-1 dual-pol (VV-VH) SAR data. The DpRVI is derived using the degree of polarization

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and the dominant normalized eigenvalue obtained from the 2×2 covariance matrix. We assess the utility of this index as an indicator of plant growth dynamics over a test site in Carman, Canada. Among the various crops grown in this region, in particular, we analyze growth stages of canola, soybean, and wheat, considering their diverse canopy structures. A temporal analysis of DpRVI with crop biophysical variables (viz., Plant Area Index – PAI, Vegetation Water Content – VWC, and dry biomass–DB) at different phenological stages confirms its trend with plant growth dynamics. The DpRVI is compared for three crops with the cross and co-pol ratio ($\sigma_{\text{VH}}^0/\sigma_{\text{VV}}^0$) and dual-pol Radar Vegetation Index ($\text{RVI} = 4\sigma_{\text{VH}}^0/(\sigma_{\text{VV}}^0 + \sigma_{\text{VH}}^0)$). Correlation analysis with biophysical variables shows that the DpRVI outperforms the other two vegetation indices with significant correlations coefficient for all three crops. For canola, DpRVI indicated the highest correlation with its biophysical variables, having a coefficient of determination (R^2) of 0.79 (PAI), 0.82 (VWC), and 0.75 (DB). Moreover, DpRVI showed a moderate correlation ($R^2 \gtrsim 0.6$) with the biophysical parameters of wheat and low biomass soybean.

Keywords: Rice, degree of polarization, RVI, PAI, DpRVI, vegetation water content

1. Introduction

Crop growth condition monitoring is a principal element for production risk estimates at a large spatial extent. Remote sensing techniques are known to provide operational crop monitoring techniques to understand crop dynamics at a local and regional level. Although optical remote sensing has been successfully used in such an operational framework (e.g., MODIS veg-

7 etation products), these systems are restricted to data acquired under clear
8 sky conditions. In this context, synthetic aperture radar (SAR) data are
9 of significant interest for agricultural applications due to the ability of SAR
10 systems to monitor crops under all weather conditions, and the sensitivity of
11 the microwave signal to the dielectric and geometrical properties of the tar-
12 get (McNairn and Shang, 2016; Steele-Dunne et al., 2017). In particular, the
13 availability of dual-pol SAR datasets from the operational Sentinel-1 mission
14 presented a unique opportunity for the remote sensing application commu-
15 nity (ESA, 2017). Dual-pol modes have advantages over full-pol acquisitions
16 in terms of larger swath width and less data volume at the expense of limited
17 polarimetric information (Lee et al., 2001; Ainsworth et al., 2009).

18 The Sentinel-1 dual-pol mode (VV-VH), refers to the transmission of
19 a vertically polarized wave with the simultaneous reception of vertical and
20 horizontal polarization. Hence, the received wave in co- and cross-polarized
21 channels (VV-VH) provides information about a target directly in terms of
22 backscatter intensities. Several studies utilized the backscatter intensities
23 for identification of crop types (Kussul et al., 2016; Nguyen et al., 2016;
24 Bargiel, 2017; Van Tricht et al., 2018; Mandal et al., 2018b; Whelen and
25 Siqueira, 2018) and crop biophysical parameter estimation (Bousbih et al.,
26 2017; Kumar et al., 2018; Mandal et al., 2018a). The sensitivity of backscatter
27 intensities to crop phenology and morphological development led to develop-
28 ing crop monitoring framework solely with scattering powers (Nelson et al.,
29 2014; Nguyen et al., 2016; Lasko et al., 2018; Singha et al., 2019; Fikriyah
30 et al., 2019).

31 Several efforts were attempted to derive vegetation metrics from SAR

32 data using backscatter intensity ratios. Blaes et al. (2006) investigated the
 33 sensitivity of $\sigma_{\text{VH}}^0/\sigma_{\text{VV}}^0$ with the growth dynamics of maize plant. At high
 34 incidence angle (35-45°), $\sigma_{\text{VV}}^0/\sigma_{\text{VH}}^0$ is sensitive to plant growth until the leaf
 35 area index (LAI) and vegetation water content (VWC) reach $4.90 \text{ m}^2 \text{ m}^{-2}$
 36 and 5.6 kg m^{-2} , respectively. Later, this ratio is aptly utilized for crop type
 37 classification (McNairn et al., 2009; Inglada et al., 2016; Denize et al., 2019),
 38 phenology estimation (McNairn et al., 2018; Canisius et al., 2018), and veg-
 39 etation characterization (Velooso et al., 2017; Vreugdenhil et al., 2018; Khab-
 40 bazan et al., 2019). Velooso et al. (2017) noticed that this ratio was relatively
 41 stable during pre-cultivation stages and increased significantly at the tillering
 42 stages of cereal crops (wheat and barley). The $\sigma_{\text{VH}}^0/\sigma_{\text{VV}}^0$ ratio is better cor-
 43 related to the fresh biomass of cereals and Normalized Difference Vegetation
 44 Index (NDVI) than the individual channel backscatter response. Besides, this
 45 ratio indicates better separability of maize, soybean, and sunflower during
 46 their heading/flowering stages.

47 The quad-pol Radar Vegetation Index (RVI) proposed by Kim and van
 48 Zyl (2009), was modified for dual-pol SAR data (Trudel et al., 2012) as,
 49 $4\sigma_{\text{HV}}^0/(\sigma_{\text{HH}}^0 + \sigma_{\text{HV}}^0)$. Later with Sentinel-1 like dual-pol data (VV-VH), few
 50 studies used the alternative formulation as, $4\sigma_{\text{VH}}^0/(\sigma_{\text{VV}}^0 + \sigma_{\text{VH}}^0)$ (Nasirzade-
 51 hdizaji et al., 2019; Gururaj et al., 2019). Nevertheless, these studies are
 52 driven by the utilization of the cross-polarized component of the received
 53 wave. Periasamy (2018) proposed the Dual Polarization SAR Vegetation In-
 54 dex (DPSVI) by investigating the physical scattering behavior of several tar-
 55 gets (vegetation, soil, urban area, and water) in co- and cross-pol channels
 56 of Sentinel-1. It calculates the rate of depolarization in terms of the verti-

cal dual depolarization index, $(\sigma_{VV}^0 + \sigma_{VH}^0)/\sigma_{VV}^0$ to separate bare soil from vegetation. The DPSVI indicated high R^2 values (>0.70) with both optical data-driven NDVI and above-ground biomass. Chang et al. (2018) utilized the degree of polarization parameter (average of HH and VV channel degree of polarizations) along with the cross-pol backscatter intensity to characterize vegetation from bare soil. It may be noted that utilizing the scattered wave information in terms of the roll-invariant degree of polarization (m) would enhance target characterization (Shirvany et al., 2012; Touzi et al., 2015, 2018).

Chang et al. (2018) utilized the degree of polarization of partially polarized waves for deriving a vegetation index (PRVI) for quad-pol SAR data. Assuming vegetation canopy as a depolarizing media, they first obtained the depolarized part by subtracting the degree of polarization from unity (i.e., $(1 - m)$), subsequently multiplying it with the cross-polarization channel intensity (σ_{HV}^0 in dB). This approach showed a good correlation of PRVI with shrubland biomass ($R^2 = 0.75$) than RVI ($R^2 = 0.50$), which usually develops random structures within the vegetation canopy. However, agricultural crops often exhibit a predefined orientation (e.g., vertical or horizontal based on erectophiles and planophiles) and row structures. In this sense, only relying on cross-polarized power may lead to issues related to backscatter intensity saturation. Hence, utilizing HV (or VH) may falsely indicate a high value of the vegetation index, even though the vegetation canopy is not entirely developed. An alternative would be to utilize the dominant scattering component (in terms of the eigenvalue spectrum of the covariance matrix) while calculating the polarized components.

82 In this present work, we utilize the dual-pol Sentinel-1 SAR data to de-
 83 rive a new radar vegetation index (DpRVI) for crop condition monitoring.
 84 The eigenvalue spectrum obtained from the eigen-decomposition of the dual-
 85 pol covariance matrix and the degree of polarization is used to derive this
 86 new index. Instead of utilizing the polarization channel backscatter intensi-
 87 ties (Chang et al., 2018; Periasamy, 2018), the proposed index utilizes the
 88 normalized dominant eigenvalue and the degree of polarization which are
 89 roll and polarization basis invariant. Moreover, DpRVI is a bounded quan-
 90 tity (between 0 and 1), unlike PRVI, which uses the channel intensity in
 91 decibel, making it unbounded. We assess the utility of the dual-pol radar
 92 vegetation index (DpRVI) as an indicator of plant growth dynamics over the
 93 Joint Experiment for Crop Assessment and Monitoring (JECAM) test site in
 94 Carman (Manitoba), Canada. We perform a comparative analysis between
 95 DpRVI, $\sigma_{\text{VH}}^0/\sigma_{\text{VV}}^0$, and dual-pol RVI for three structurally diverse crop types.
 96 We further assess the temporal response of DpRVI to vegetation dynamics
 97 by comparing them with the in-situ measured vegetation biophysical param-
 98 eters, such as Plant Area Index (PAI), Vegetation Water Content (VWC),
 99 and Dry biomass (DB).

100 2. Study area and dataset

101 The present study is carried over the Joint Experiment for Crop Assess-
 102 ment and Monitoring (JECAM) test site in Carman, Manitoba (Canada), as
 103 shown in Fig. 1. The test site covers approximately $26 \times 48 \text{ km}^2$ of the area
 104 and is characterized by various agricultural crop types and soil conditions.
 105 The major annual crops grown in this area include wheat, canola, soybeans,

106 corn, and oats. Only a small fraction ($<5\%$) is under grassland and pasture.
 107 The in-situ measurements were collected over the area near coincident with
 108 satellite passes during the Soil Moisture Active Passive Validation Experiment (SMAPVEX16-MB) campaign in 2016 (Bhuiyan et al., 2018).

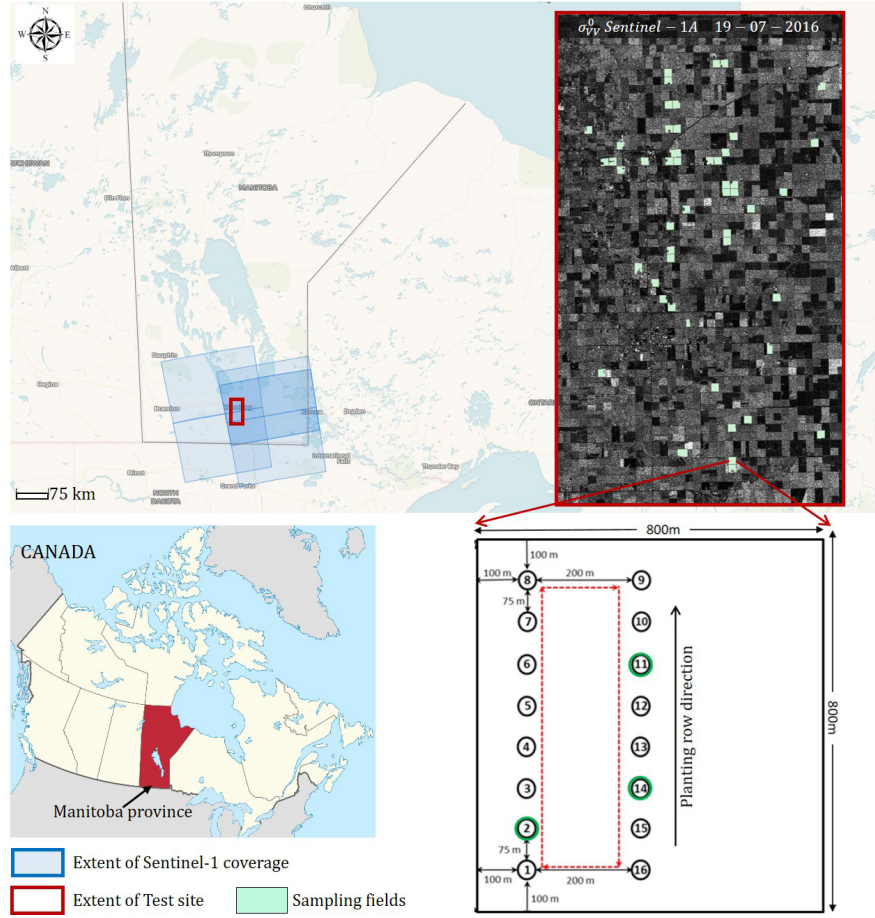


Figure 1: Study area (red box) and Sentinel-1 passes (blue boxes) over the Carman JECAM test site. The sampling fields (mint green polygons) are overlaid on σ_{VV}^0 Sentinel-1A image of 19 July, 2016. A layout of 16 sampling locations within a field is highlighted.

109
 110 During the campaign, in-situ measurements of vegetation and soil were
 111 collected in two distinct periods (June 08 to June 22, and July 8 to July 22,

112 2016) over 50 agricultural fields. During this experimental period, most of
 113 the crops advanced from an early stage to a peak accumulation of biomass
 114 at the full vegetative stage, as shown in Fig. 2. The nominal size of each
 115 field is approximately 800 m×800 m. In each sampling field, three points
 116 were selected for vegetation sampling, as shown in Fig. 1, which included
 117 measurement of plant area index (PAI), wet and dry biomass, plant height,
 118 and phenological stages through destructive and non-destructive sampling
 119 methods (McNairn et al., 2016). The biomass measurements are used to
 120 derive the vegetation water content (VWC) and dry biomass (DB) per unit
 square meter area.

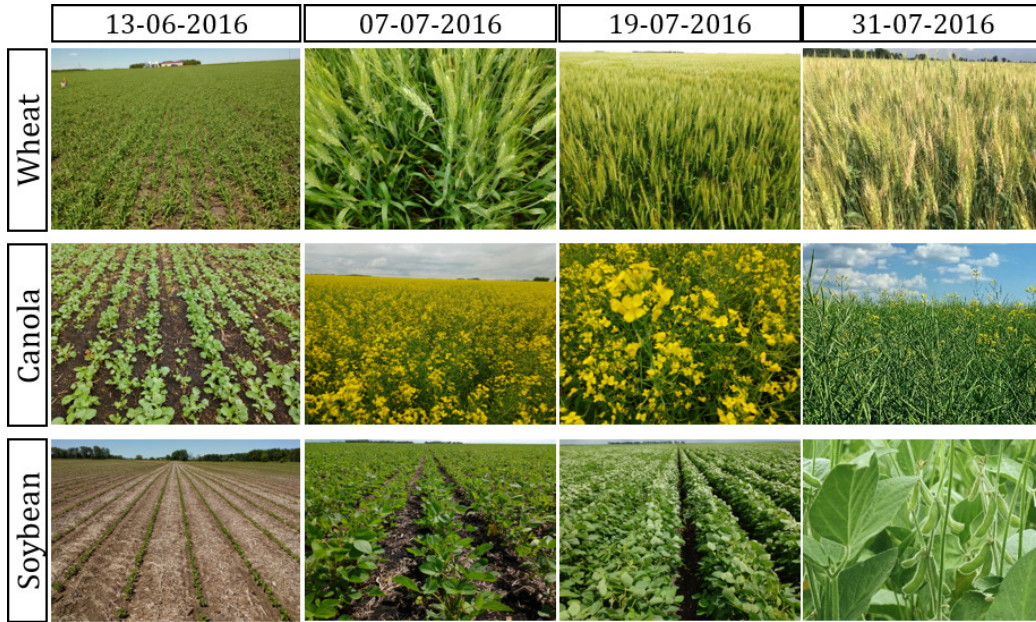


Figure 2: Field condition during the campaigns for wheat, canola, and soybean crops.

121

122 An illustration of vegetation and soil sampling methods during the field
 123 campaigns can be found in SMAPVEX16-MB experiment report (McNairn

et al., 2016). Among several Sentinel-1 acquisitions during the campaign, four dual polarization (VV and VH) C-band Sentinel-1A Single Look Complex (SLC) data used in this study, as given in Table 1. The selection of Sentinel-1 data is solely based on acquisition dates and in-situ measurements periods.

Table 1: Sentinel-1A acquisitions over Carman test site during the field campaign

Acquisition date	Beam Mode	Incidence Angle Range (deg.)	Orbit
13/06/2016	IW	31.32–35.24	Ascending
07/07/2016	IW	31.12–35.54	Ascending
19/07/2016	IW	31.12–35.54	Ascending
31/07/2016	IW	31.12–35.54	Ascending

3. Methodology

3.1. SAR data preprocessing

Sentinel-1 acquires data over land majorly in the Terrain Observation with Progressive Scans SAR (TOPSAR) mode and delivers the Level-1 SLC data in Interferometric Wide (IW) product. A full swath covers approximately 250 km length at 5×20 m spatial resolution in single look. The IW swath consists of three sub-swaths (IW1, IW2, and IW3) in the range direction. Each sub-swaths has 9 bursts in the azimuth direction, and the individually focused complex bursts are arranged in azimuth-time order with black-fill in between. For further applications, these SLC products are pre-processed with a standard set of corrections in a workflow, as shown in Fig. 3.

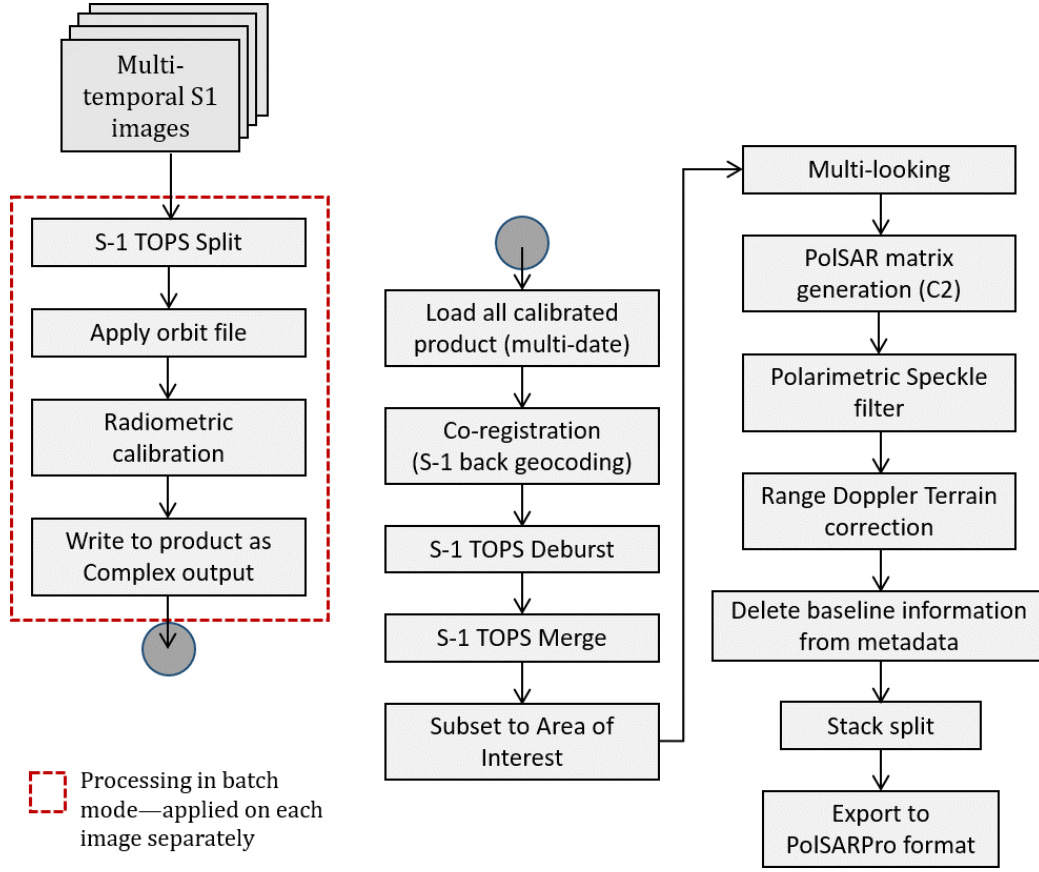


Figure 3: Sentinel-1 preprocessing workflow for time-series data.

141 The present study involves preprocessing of the temporal dataset to ob-
 142 tain the 2×2 covariance matrices. Individual Sentinel-1 images are read into
 143 the SNAP7.0 tool (ESA, 2015) provided by ESA. The sub-swaths and bursts
 144 are then selected based on the test area coverage with TOPS Split module. A
 145 precise orbit file is applied to update the state vectors, and subsequently, the
 146 images are calibrated. Unlike the GRD processing pipeline, which is used to
 147 generate the radar cross-section powers (σ^0), the current workflow requires
 148 saving the radiometric calibration output product in a complex-valued for-

149 mat. A complex-values output is necessary to generate the covariance matrix
150 in succeeding steps. These processing steps are performed in a batch mode
151 for all temporal datasets.

152 All these calibrated images from different dates are coregistered using
153 the S-1 Back Geocoding module to generate a stack of coregistered data.
154 This interferometric coregistration module coregisters all the SLC images
155 with sub-pixel accuracy using a digital elevation model (DEM) and orbit
156 information. Subsequently, the stack of temporal images is processed for
157 Sentinel-1 TOPS Deburst and TOPS Merge, which merges different bursts
158 of an individual image (of a particular date) into a single SLC image. Subset
159 operation is then performed on the deburst image to clip the product into
160 smaller spatial extent covering the test area.

161 The subset stacked images are multilooked by 4×1 in range and azimuth
162 direction to generate ground ranged square pixels. These multi-looked prod-
163 ucts are then utilized to produce a 2×2 covariance matrix (\mathbf{C}_2). The matrix
164 elements are further processed by despeckling them with a 5×5 Refined Lee
165 filter. These elements are subsequently geocoded to a UTM projected coor-
166 dinate systems using the Range Doppler Terrain correction. The next step
167 requires the deletion of baseline information from the metadata, which is
168 essential for exporting the covariance matrices from SNAP to PolSARPro
169 format. The stack is then split into individual products using Stack Split op-
170 erator, and these products (i.e., the 2×2 covariance matrices for single dates)
171 are exported into the PolSARPro format. It stores each matrix elements
172 (C_{11} , C_{22} , $\Re(C_{12})$, and $\Im(C_{12})$) individually in a binary format with separate
173 header information. These elements essentially deal with the second-order

174 scattering information generated from the spatial averaging of the scattering
 175 vector $k = [S_{VV}, S_{VH}]^T$ as expressed in (1),

$$\mathbf{C}_2 = \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & \langle S_{VV} S_{VH}^* \rangle \\ \langle S_{VH} S_{VV}^* \rangle & \langle |S_{VH}|^2 \rangle \end{bmatrix} \quad (1)$$

176 where superscript $*$ denotes complex conjugate and $\langle \dots \rangle$ denotes spatial av-
 177 erage over a moving window.

178 3.2. Dual-pol Radar Vegetation Index (DpRVI)

179 Radar backscatter intensity provides information about spatial and tem-
 180 poral variations in crop growth and their phenology stages. Hence, assim-
 181 ilating time-series SAR data for crop growth monitoring could improve risk
 182 assessment. A reasonable step in this regard would be to derive various vege-
 183 tation metrics from SAR data. While utilizing the characteristic of scattering
 184 randomness from vegetation structure, few studies proposed radar vegetation
 185 indices viz., RVI (Kim and van Zyl, 2009), and GRVI (Mandal et al., 2020)
 186 for full-pol SAR data to provide a relatively simple and physically inter-
 187 pretable vegetation descriptor. Even though these radar vegetation indices
 188 are a good proxy for vegetation condition, they are confined to the use of
 189 full-polarimetric SAR data. Hence, there is a need to devise a vegetation
 190 index for dual-pol SAR data (viz., Sentinel-1).

191 In this study, we have jointly utilized the scattering information in terms
 192 of the degree of polarization and the eigenvalue spectrum to derive a new
 193 vegetation index from dual-pol SAR data. The state of polarization of an
 194 EM wave is characterized in terms of the degree of polarization ($0 \leq m \leq 1$).
 195 The degree of polarization is defined as the ratio of the (average) intensity of

the polarized portion of the wave to that of the (average) total intensity of the wave. For a completely polarized EM wave, $m = 1$ and for a completely unpolarized EM wave, $m = 0$. In between these two extreme cases, the EM wave is assumed to be partially polarized, $0 < m < 1$.

Barakat (Barakat, 1977) provided an expression of m for the $N \times N$ covariance matrix. This expression is used in this study to obtain the degree of polarization m from the 2×2 covariance matrix \mathbf{C}_2 for dual-pol data as,

$$m = \sqrt{1 - \frac{4|\mathbf{C}_2|}{(\text{Tr}(\mathbf{C}_2))^2}} \quad (2)$$

where Tr is the matrix trace operator (i.e., the sum of the diagonal elements) and $|\cdot|$ is the determinant of a matrix. The two non-negative eigenvalues ($\lambda_1 \geq \lambda_2 \geq 0$) are obtained from the eigen-decomposition of the \mathbf{C}_2 matrix which are then normalized with the total power Span ($\text{Tr}(\mathbf{C}_2) = \lambda_1 + \lambda_2$). These two quantities are then utilized to derive the dual-pol radar vegetation index (DpRVI) as given in (3).

$$\text{DpRVI} = 1 - m \cdot \beta, \quad 0 \leq \text{DpRVI} \leq 1, \quad (3)$$

where $\beta = \lambda_1/\text{Span}$.

The rationale behind the joint utilization of m and β is inherited from their differential sensitivity to crop growth dynamics. The variations in scattering mechanisms associated with the phenological growth stages are combined in the present study through these two parameters. The experimental plots shown in Fig. 4 indicate their variations through temporal growth stages for three different crops.

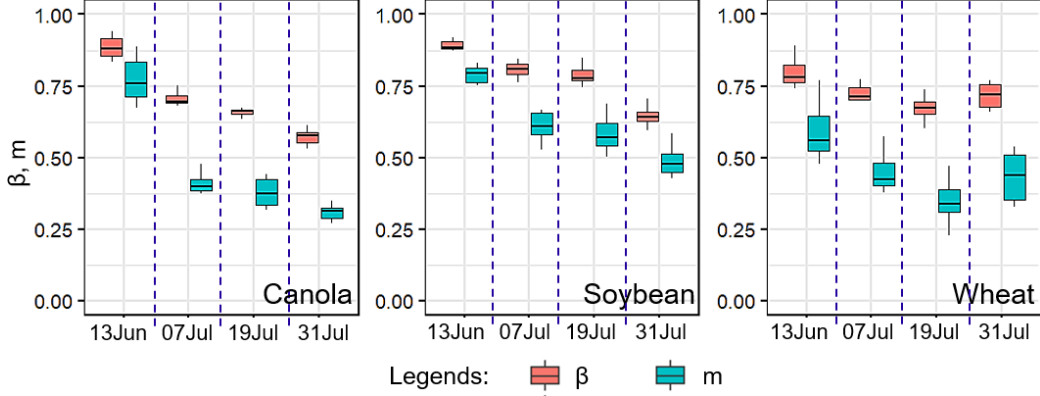


Figure 4: Sensitivity of m and β parameter in temporal scale for individual crops.

Even though these parameters are investigated in detail in Sec. 4, here, we briefly highlight their individual importance to characterize the proposed index. This insight is particularly vital considering their differential changes within a distinctive dynamic range at several phenological stages. For example, the mean values of m and β decrease with the growth stages of canola (Fig. 4). It is interesting to note that both m and β are > 0.70 with a marginal difference between their values on 13 June. However, this difference increases as canola advances through its phenology to full vegetative growth during the 3rd week of July. Similarly, for soybean and wheat, the differential sensitivities of m and β are apparent throughout its growth stages, as shown in Fig. 4. It is interesting to note that unlike other crops, wheat shows an increasing trend in both m and β during the end of the ripening stage on 31 July, with higher variations. Such a difference may be due to a high degree of randomness in scattering from wheat heads. Besides, during the end of the ripening stage (i.e., when the heads and tillers become drier), there could be a notable backscatter contribution from the ground, which

232 indicates higher values of β .

233 It can be observed from the general analysis of the eigenvalue spectrum
234 (given in Appendix A) that these differential variations between m and β
235 are related to λ_2/Span . This quantity is related to the noise associated with
236 the less dominant scattering mechanism. Usually, at the early stage of plant
237 development, there exists a single dominant scattering mechanism from the
238 bare soil, thereby showing a low difference between m and β .

239 The elements of DpRVI (i.e., m and β) are shown in a polar plot (Fig. 5).
240 This type of representation is adopted in this study to better comprehend
241 subtle variations in the scattering characteristics during the transition of phe-
242 nological stages. In this plot, $\cos^{-1} \beta$ is represented in the angular direction,
243 while m is the radial axis. In this study, the polar plot is used to characterize
244 temporal variations in the scattering attributes for each crop type, individ-
245 ually discriminated by m and β . Besides, elementary targets are shown to
246 be located at the extremities of the boundaries, while natural targets reside
247 within the polar plot.

248 The β parameter indicates the contribution of the dominant scattering
249 component withing the total power. For pure or point target scattering with
250 a dominant scattering mechanism, $\beta = 1$ which assigns to $\cos^{-1} \beta = 0^\circ$ with
251 $m = 1$ in the polar plot. This state corresponds to Case-2 shown in Fig. 5 with
252 DpRVI = 0. Theoretically, for a smooth bare surface (i.e., Bragg scattering),
253 $\lambda_1 \gg \lambda_2$ with a high value of m pointing to $\cos^{-1} \beta \approx 0$. However, the
254 cluster density plot of bare soil indicates variations in m and $\cos^{-1} \beta$ about
255 their respective extremes, which is possible for natural surfaces.

256 In the case of completely random scattering (i.e., with no polarization

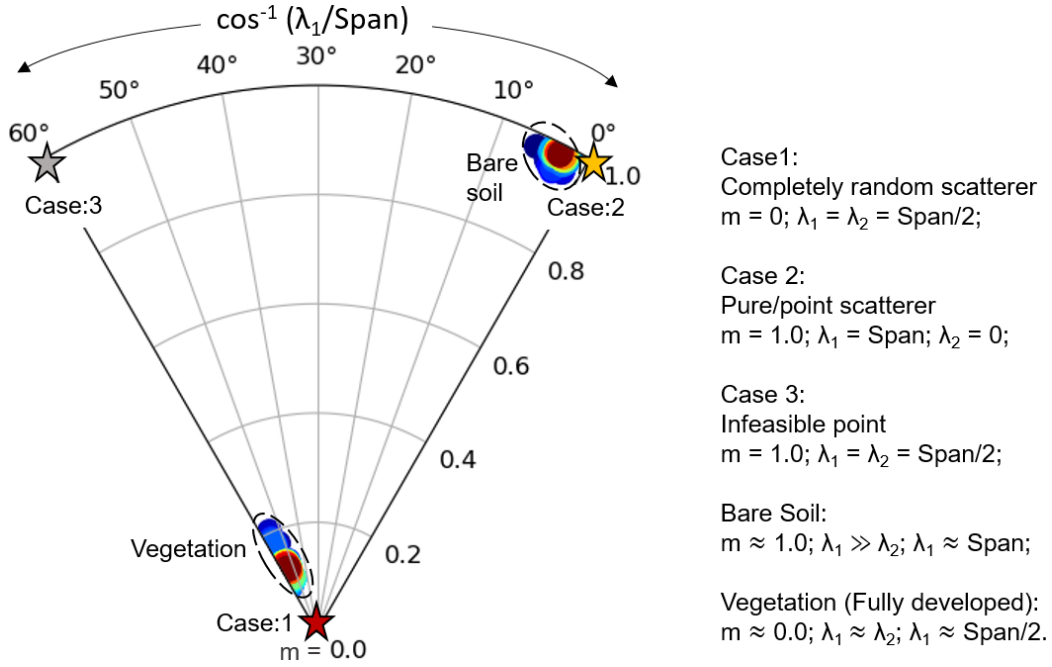


Figure 5: The elements of DpRVI i.e., degree of polarization (m) and β (i.e., λ_1/Span) in polar plot. The $\cos^{-1} \beta$ is represented in the angular direction and m in radial axis of the polar plot. The boundary cases and regions of natural targets are highlighted. The vegetation and soil clusters are derived using radar measurements over the sampling fields.

structure), $m = 0$ (i.e., completely depolarized wave) and $\beta = 0.5$. This suggests that $\lambda_1 = \lambda_2 = \text{Span}/2$ for which $\text{DpRVI} = 1$. Case-1 is a typical example of such a state. However, for natural targets like fully developed vegetation canopy, $m \approx 0$ and $\beta \approx 0.5$, leading to higher DpRVI, i.e., $\text{DpRVI} \approx 1$. Moreover, dispersion of m and β in the density plot is evident in the vegetation cluster. As plant canopy advances from early leaf development to fully vegetative stage, the DpRVI increases from 0 to 1.

It can be noted that at each phenological stage, m and β is denoted as points in the polar plot. However, certain regions in the $m - \beta$ plot are infeasible due to the non-existence of physical depolarizers in such regions.

Case-3 is an instance of such a state, where $m = 1.0$ (i.e., pure target) and $\cos^{-1}\beta = 60^\circ$, indicating, $\lambda_1 = \lambda_2 = \text{Span}/2$ (i.e., similar to a complete depolarizer). These types of targets are not practically possible in natural scenarios.

3.3. Data analysis and comparison

Elements of the \mathbf{C}_2 matrix are used to calculate the DpRVI as discussed in Sec. 3 for each acquisition over a 5×5 window. In addition, the DpRVI is compared with the cross and co-pol ratio ($\sigma_{VH}^0/\sigma_{VV}^0$) and the RVI ($4\sigma_{VH}^0/(\sigma_{VV}^0 + \sigma_{VH}^0)$). These parameters are computed from the diagonal elements of the \mathbf{C}_2 matrix. The in-situ measurement points (i.e., the vector file) are overlayed on the temporal $\sigma_{VH}^0/\sigma_{VV}^0$, and RVI and DpRVI images. Here it is important to note that the nominal field size of the study area is relatively bigger (approx. $800\text{ m} \times 800\text{ m}$) than the size of the image pixel (approx. $15\text{ m} \times 15\text{ m}$). Hence, the vegetation indices for each sampling location are calculated as an average over a 3×3 window centered on each site.

These parameters are initially investigated on a temporal scale for various phenological stages of crops. We have selected three structurally different crops for this study: wheat, canola, and soybean. The temporal behaviour of these parameters are also compared with crop biophysical variables, such as the plant area index (PAI, m^2m^{-2}), dry biomass (DB, kgm^{-2}), and vegetation water content (VWC, kgm^{-2}). Finally, the DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$, and RVI are utilized in a correlation analysis with these crop biophysical variables.

289 4. Results and discussion

290 This section describes the results of the proposed vegetation index–DpRVI
291 separately for three crop types, viz., canola, soybean, and wheat. Besides,
292 the comparative investigation of DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$, and dual-pol RVI are
293 assessed along with crop biophysical parameters in this section.

294 4.1. Canola

295 The temporal analysis of DpRVI averaged for three sampling points in
296 each canola fields (Field no. 206, 208, and 224) are shown in Fig. 6. For
297 comparative analysis, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI for these fields are presented. Fur-
298 thermore, a regression analysis is performed for the vegetation indices with
299 in-situ measured PAI, VWC, and dry biomass (Fig. 8).

300 The in-situ measurements indicate that canola seeding was almost com-
301 pleted by the 3rd week of May. Thus, plant development during the beginning
302 of June was primarily limited to vegetative growth. Subsequently, flowering
303 started in the last week of June to early July, which led to pod development
304 by the mid of July. Ripening of seeds and senescence followed at the end of
305 July until the 2nd week of August. The phenological stages are highlighted
306 in the temporal plots of vegetation indices for each field (Fig. 6). Analysis of
307 canola, in particular, is interesting due to its dynamic morphological changes
308 with phenology. Canola is a broad-leaf plant with distinctive differences in
309 canopy structure throughout the growing season. Upon emergence, the plant
310 develops a dense rosette of leaves near to the soil. Hence, the backscatter
311 response is affected by the development of leaves, which have a similar size
312 compared to C-band wavelength (≈ 5.6 cm). The canola stem then bolts,

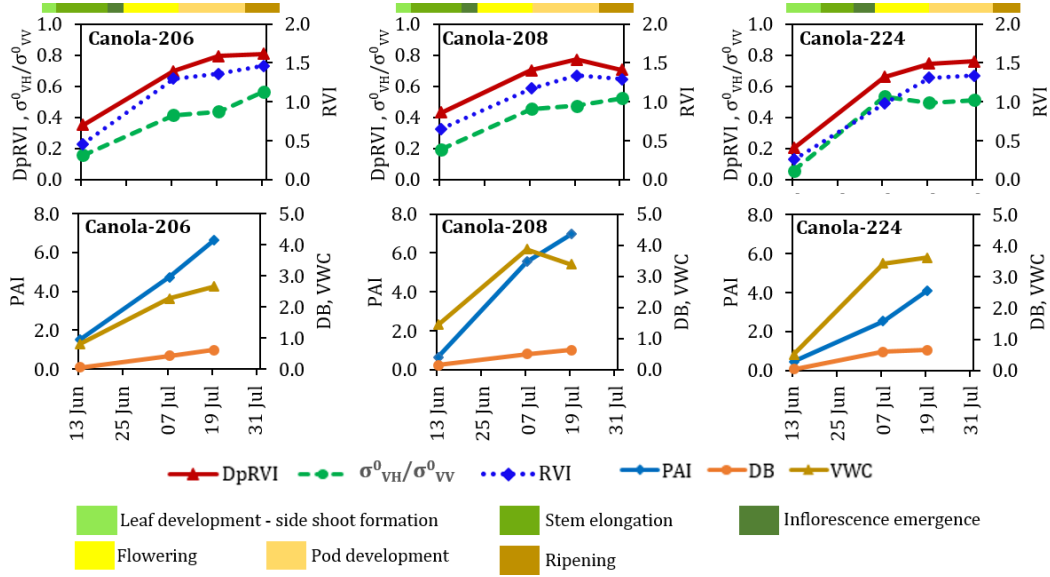


Figure 6: Temporal pattern of vegetation indices ($DpRVI$, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI) for three representative canola fields at different growth stages. The in-situ measurements of Plant Area Index (PAI , $m^2 m^{-2}$), Vegetation water content (VWC , $kg m^{-2}$), and dry biomass (DB , $kg m^{-2}$) are plotted in second row for each field.

313 increasing its vertical structure just before flowering and podding with the
 314 increase in both PAI and biomass (Wiseman et al., 2014). Latter in the pod
 315 development stage, it usually forms a dense and complex canopy structure.

316 On 13 June, $DpRVI$ is ≈ 0.35 in the majority of the canola fields, indicat-
 317 ing low vegetation content. In-situ measurements confirm that their growth
 318 was limited to the stem elongation stage with low PAI ($\approx 1.45 m^2 m^{-2}$) and
 319 biomass ($VWC = 1.0 kg m^{-2}$ and $DB < 0.2 kg m^{-2}$). The vegetation cluster
 320 in the $m - \beta$ polar plot (Fig. 7 shows a high value of $m \approx 0.90$ along with
 321 a high value of β ($\cos 20^\circ = 0.94$) during early development stages with less
 322 random canopy structure. Similarly, a low value of $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI also
 323 indicate sparse vegetation condition. In comparison to field 206 and 208,

324 with low vegetation cover (i.e., $\text{PAI} \approx 0.5 \text{ m}^2 \text{ m}^{-2}$) and $\text{VWC} < 0.42 \text{ kg m}^{-2}$),
 325 a lower value of DpRVI (≈ 0.18) is apparent in field 224, where the canola
 plants were still at their leaf development stage.

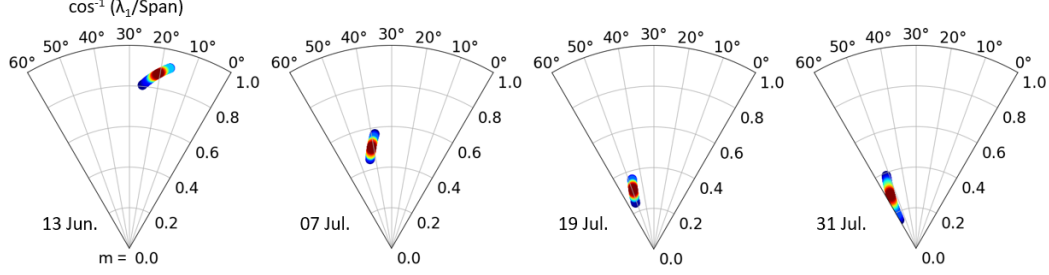


Figure 7: Temporal variations of degree of polarization (m) and β in polar plots for canola fields.

326

327 The DpRVI values for each field increased rapidly as the plant growth
 328 progresses from the early vegetative stage to the beginning of pod devel-
 329 opment. During the early pod development stage (19 July), the DpRVI is
 330 $\approx 0.8 \pm 0.04$. At high growth stages, with the increase of vegetation ele-
 331 ments, a decrease in m is likely due to the depolarization of incident waves
 332 from the complex vegetation canopy. During this pod development stage,
 333 the ramified stems and the randomly oriented pods create a complex upper
 334 canopy structure that may increase multiple scattering mechanisms. This
 335 aspect may lead to similar values of λ_1 and λ_2 (equal to $\text{Span}/2$). Variations
 336 in m and β with vegetation growth stages are apparent in Fig. 7. A signifi-
 337 cant increase in $\sigma_{VH}^0/\sigma_{VV}^0$ is observed during the inflorescence emergence and
 338 flowering stage. This event can be possibly explained by the changes in the
 339 cross-pol intensity as the canopy develops (Pacheco et al., 2016).

340 During the advanced pod development to ripening stage, the DpRVI val-

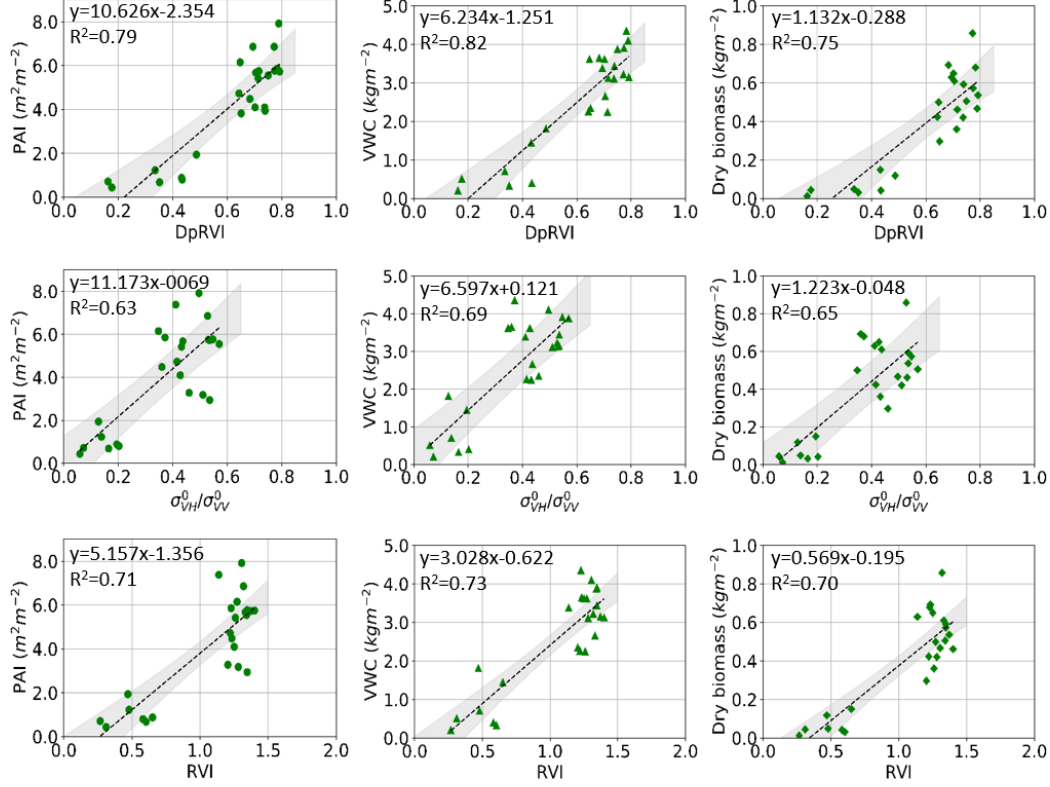


Figure 8: Correlation analysis between vegetation indices (DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI) and crop biophysical parameters, i.e., Plant Area Index (PAI, $\text{m}^2 \text{m}^{-2}$), Vegetation water content (VWC, kg m^{-2}), and dry biomass (DB, kg m^{-2}) for canola. The linear regression line is indicated as black dashed line. The 95% confidence limits are highlighted as gray regions.

ues are peculiarly confined within the range of 0.75 ± 0.05 , rather than increasing from the early pod development stages. At the end of the pod development stage, in-situ measurements indicate high vegetation cover ($\text{PAI} \approx 6.0 \text{ m}^2 \text{m}^{-2}$) and biomass ($\text{VWC} > 3.0 \text{ kg m}^{-2}$ and $\text{DB} \approx 1.0 \text{ kg m}^{-2}$). The sensitivity of the SAR signal to the accumulation of biomass from leaf development until the flowering stage is apparent in Fig. 6. Following this, a saturation of the C-band signal is likely due to the high volume of vegetation components dur-

ing the pod development stage (Wiseman et al., 2014). Besides, the values of $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI also remain stable at high growth stages. These results are comparable to the backscatter response from canola reported in Veloso et al. (2017); Vreugdenhil et al. (2018).

Furthermore, a quantitative assessment of vegetation indices is essential for comparative analysis. The correlation plots in Fig. 8 indicate that the DpRVI values are better correlated with the biophysical parameters of canola than $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI. It is observed that the coefficients of determination (R^2) for the PAI, VWC, and DB with DpRVI are 0.79, 0.82, and 0.75 respectively. Hence, it can be seen that in particular, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI showed a relatively lower correlation with PAI, VWC, and DB. The DpRVI indeed outperforms the other two vegetation indices with a stronger correlation, with low variance throughout the entire growth stages.

4.2. Soybean

Unlike cereal and oil-seed crops, soybean (belongs to the leguminous family of crops) has more planophile canopy architecture. However, at the high vegetative stage, the canopy develops a random structure. This is due to its unique morphology with trifoliate leaf (a compound leaf made of three leaflets) attached to each stem node with petiole, secondary stems, and randomly oriented leaves (Fehr et al., 1971).

The Manitoba weekly crop reports (Agriculture, 2016) suggests that soybean seeding was completed by the 3rd week of May. Thus, crop development during the beginning of the SMAPVEX-16 campaign in June was primarily restricted to vegetative growth. Subsequently, inflorescence emergence, flowering, and pod initiation started during the last week of July. The develop-

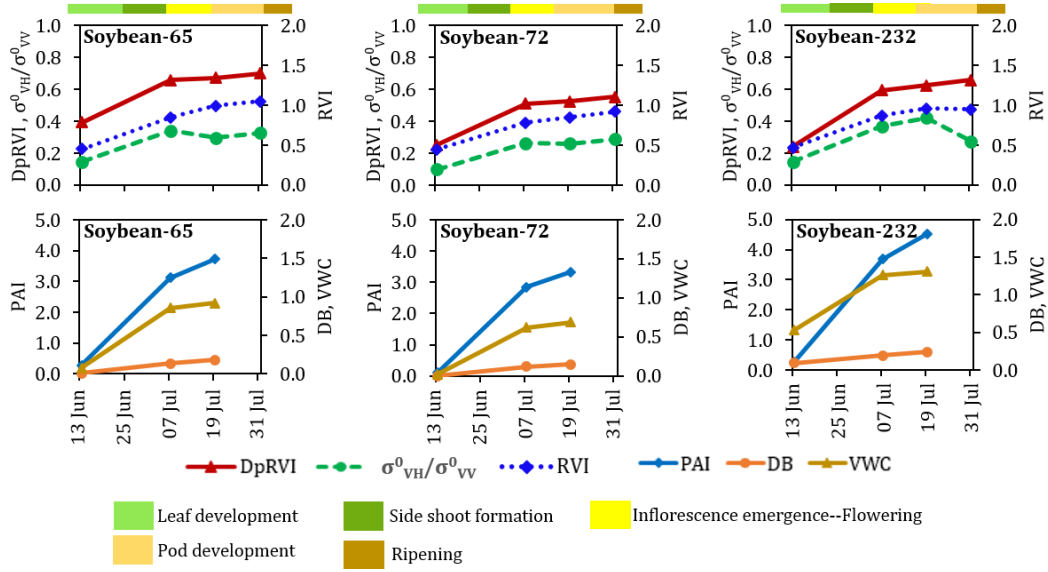


Figure 9: Temporal pattern of vegetation indices (DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI) for three representative soybean fields at different growth stages. The in-situ measurements of Plant Area Index (PAI, $\text{m}^2 \text{m}^{-2}$), Vegetation water content (VWC, kg m^{-2}), and dry biomass (DB, kg m^{-2}) are plotted in second row for each field.

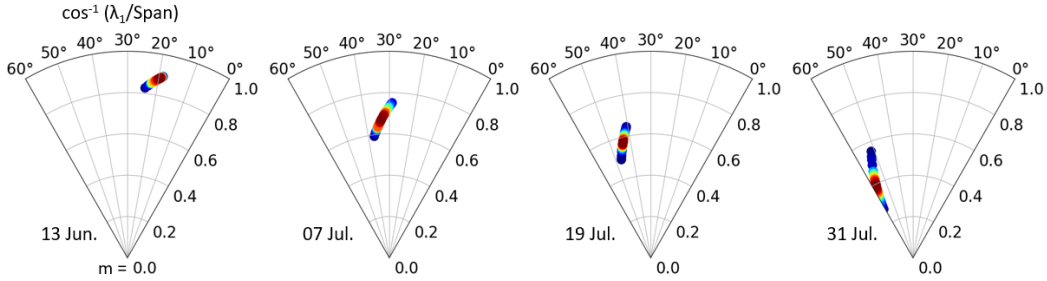


Figure 10: Temporal variations of degree of polarization (m) and β in polar plots for soybean fields.

373 ment of pods, ripening of seeds, and senescence followed in August until the
374 2nd week of September.

375 Fig. 9 shows the temporal trends of the vegetation indices for three rep-

376 resentative fields (Field no. 65, 72, and 232). It is evident from Fig. 9 that
 377 the DpRVI values for each field increase rapidly as the vegetation growth
 378 increases from the early leaf development stage to the beginning of pod de-
 379 velopment. The DpRVI value is ≈ 0.21 at the leaf development stage (on 13
 380 June).

381 In-situ measurements confirm the vegetative growth with low PAI ($\approx 0.35 \text{ m}^2 \text{ m}^{-2}$)
 382 and biomass ($\text{VWC} = 0.2 \text{ kg m}^{-2}$ and $\text{DB} < 0.05 \text{ kg m}^{-2}$). The $m - \beta$ polar
 383 plot (Fig. 10 indicates that the vegetation cluster lies in the region of high
 384 m (≈ 0.90) and β during early development stages (i.e., 2nd trifoliate stage)
 385 with less random canopy structure. During this stage, the SAR backscatter is
 386 majorly affected by the underlying soil (Wang et al., 2016). It may be noted
 387 that a similar effect of soil on backscatter response at the early vegetative
 388 stage is also reported by Cable et al. (2014) with quad-pol RADARSAT-
 389 2 SAR data. Alongside, low values of $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI also indicate an
 390 early stage of vegetation growth. However, Veloso et al. (2017) reported a
 391 higher standard deviation of the co-pol channel than cross-pol for bare soil
 392 conditions, which may impart bias in $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI values.

393 With the increase in vegetation components, the variations in DpRVI
 394 values among several fields are apparent. It reaches a high value (≈ 0.55)
 395 at the end of the flowering stage. This stage indicates an increase in the
 396 volume scattering component. Moreover, biophysical parameters are high
 397 ($\text{PAI} > 3.0 \text{ m}^2 \text{ m}^{-2}$, $\text{VWC} > 1.25 \text{ kg m}^{-2}$, and $\text{DB} > 0.40 \text{ kg m}^{-2}$) during this
 398 stage. Wigneron et al. (2004) indicated random scattering behaviour at high
 399 vegetative growth of soybean rather than a dominant scattering component.
 400 A significant increase in $\cos^{-1} \beta$ along with a decrease in m at the high vege-

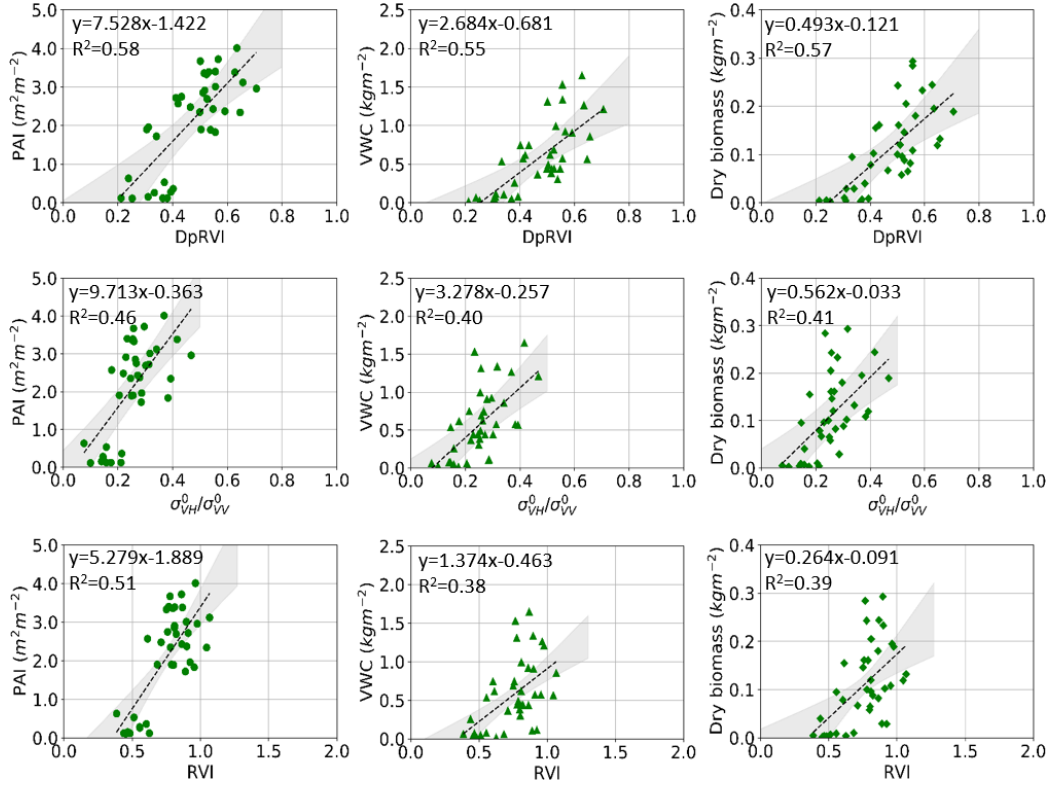


Figure 11: Correlation analysis between vegetation indices (DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI) and crop biophysical parameters, i.e., Plant Area Index (PAI, $\text{m}^2 \text{m}^{-2}$), Vegetation water content (VWC, kg m^{-2}), and dry biomass (DB, kg m^{-2}) for soybean. The linear regression line is indicated as black dashed line. The 95% confidence limits are highlighted as gray regions.

401 tation growth stage (Fig. 10 are in agreement with these findings. Conversely,
 402 variations in $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI values are higher than DpRVI, which is likely
 403 due to lower attenuation of the co-pol channel at pod development stages.

404 The correlation plots in Fig. 11 indicate that DpRVI values are better
 405 correlated with the biophysical parameters than $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI. The co-
 406 efficients of determination (R^2) for PAI, VWC, and DB with DpRVI are 0.58,
 407 0.55, and 0.57, respectively. Even though the correlations are statistically sig-

408 nificant, the R^2 values are lower than that of canola (Fig. 8). This aspect is
409 likely because the vegetation indices derived for low biomass soybean canopy
410 is highly affected by the underlying soil rather than the vegetation canopy.

411 4.3. *Wheat*

412 Compared to canola and soybean, wheat belongs to the graminaceous
413 family, which is characterized by erectophile (canopy elements have predom-
414 inant vertical distribution) architecture. Thus this morphological diversity is
415 characterized by distinctive backscatter responses and associated vegetation
416 indices. In the test site, wheat was sown during the start of May. Most fields
417 were at the tillering stage on 13 June and then advanced to the heading stage
418 by the end of June. Subsequently, flowering, fruit development started during
419 the mid-week of July. The onset of dough and maturity stages began at the
420 end of July. The corresponding vegetation indices derived from time-series
421 Sentinel-1 data are shown in Fig. 12.

422 Variations in DpRVI values among three representative fields (Field no.
423 220, 233, and 62) are evident with vegetation growth. Lowest DpRVI values
424 are observed when wheat advanced from the leaf development to the tillering
425 stage on 13 June. Fields with plant density (PD) of $\approx 100 \text{ m}^{-2}$ (Fields no. 220)
426 have low DpRVI values (≈ 0.22), which are comparatively lower than wheat
427 fields (Field no. 233 and 62) with high PD (125 m^{-2} and 190 m^{-2}). In-situ
428 measurements of PAI and VWC are also relatively higher ($> 2.5 \text{ m}^2 \text{ m}^{-2}$ and
429 $\approx 1.1 \text{ kg m}^{-2}$) for wheat fields with high plant density. In comparison to other
430 crops, wheat gained more vegetative components on 13 June, which lead to
431 higher DpRVI values. The $m - \beta$ polar plot (Fig. 13) also show moderate to
432 high values of m (≈ 0.65) and β ($\cos 35^\circ = 0.82$) on 13 June.

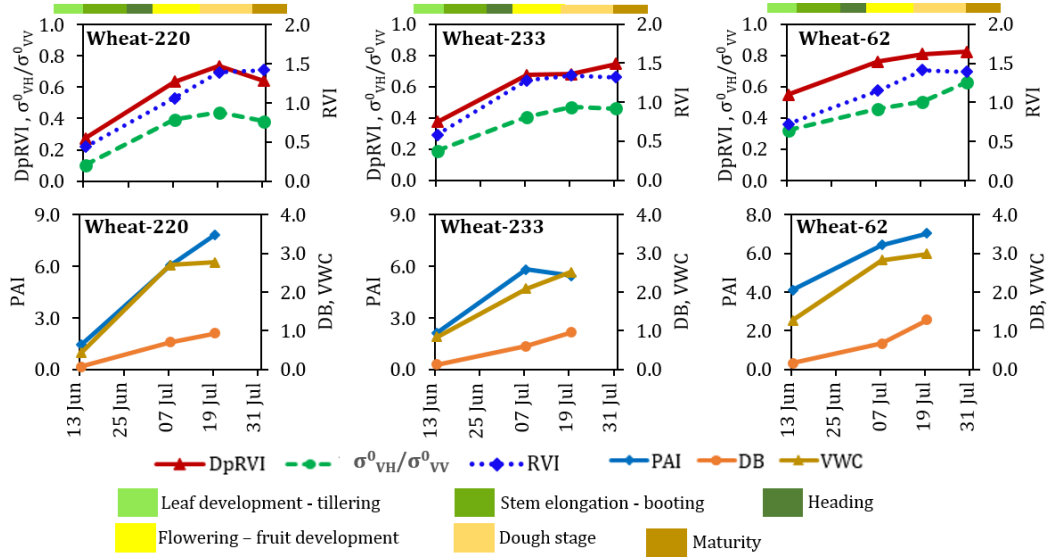


Figure 12: Temporal pattern of vegetation indices (DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI) for three representative wheat fields at different growth stages. The in-situ measurements of Plant Area Index (PAI, $\text{m}^2 \text{m}^{-2}$), Vegetation water content (VWC, kg m^{-2}), and dry biomass (DB, kg m^{-2}) are plotted in second row for each field.

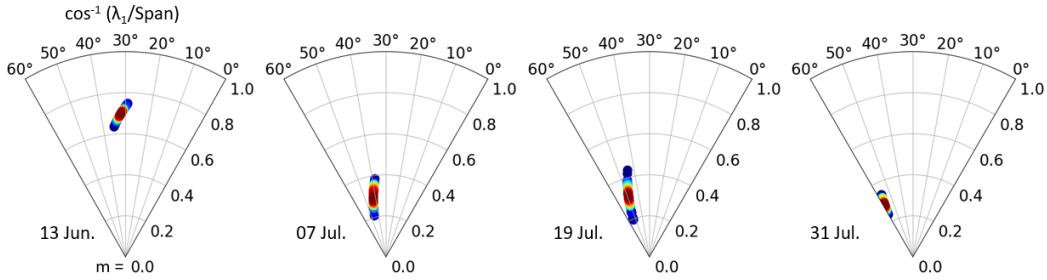


Figure 13: Temporal variations of degree of polarization (m) and β in polar plots for wheat fields.

433 The DpRVI values reached its maximum when the crop advanced from
 434 flowering to early dough stages on 19 July. DpRVI reaches up to 0.74 for low
 435 PD fields (Field no. 220), while these values peak at ≈ 0.8 for fields with
 436 high PD (Field no. 233 and 62). This difference may be due to the high

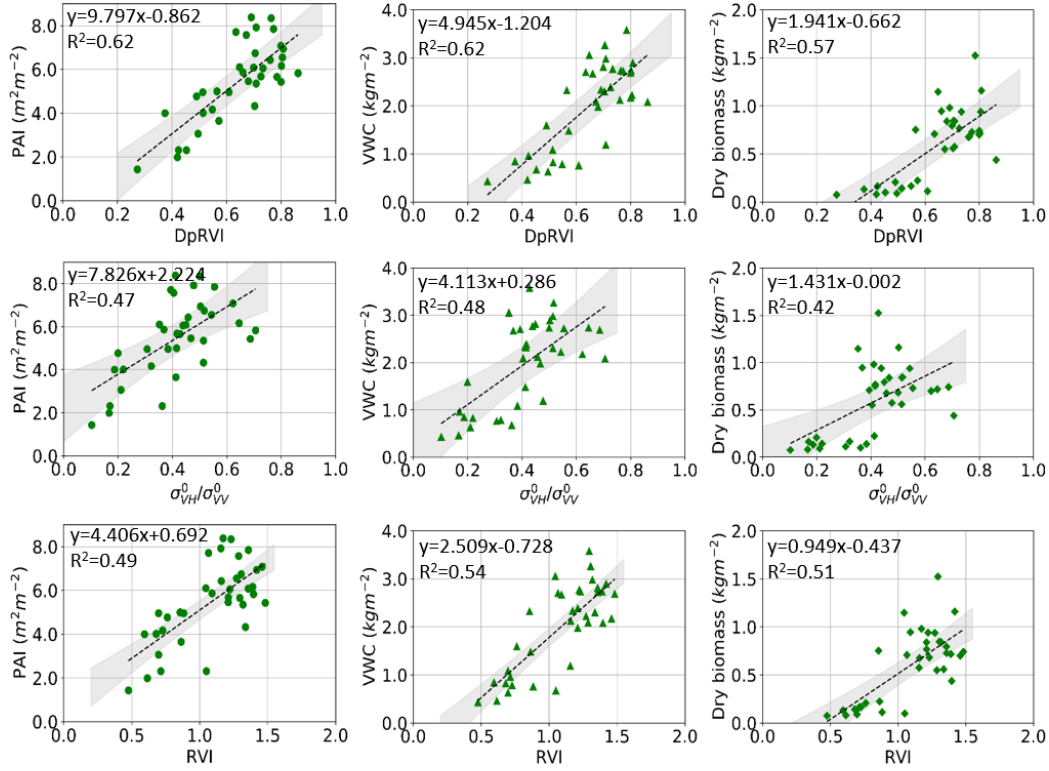


Figure 14: Correlation analysis between vegetation indices (DpRVI, $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI) and crop biophysical parameters, i.e., Plant Area Index (PAI, $\text{m}^2 \text{m}^{-2}$), Vegetation water content (VWC, kg m^{-2}), and dry biomass (DB, kg m^{-2}) for wheat. The linear regression line is indicated as black dashed line. The 95% confidence limits are highlighted as gray regions..

437 degree of randomness in scattering ($m \approx 0.35$ and $\cos^{-1} \beta \approx 50^\circ - 55^\circ$ on
 438 19 July) from the canopy elements during the flowering to fruit development
 439 stages. In-situ measurements of plant biophysical parameters at these stages
 440 confirm their increment up to approximately 6.2 to $8.1 \text{ m}^2 \text{m}^{-2}$, 3.0 kg m^{-2} ,
 441 and 1.1 kg m^{-2} , for PAI, VWC, and DB, respectively. This indicates high
 442 multiple scattering from the canopy which might lead to $\lambda_1 \approx \lambda_2 \approx \text{Span}/2$
 443 (i.e., no dominant scattering) with low values of m (≈ 0.25). The differential

444 increase in DpRVI among the wheat fields is visible in Fig. 12. Variations
 445 in plant density might cause a difference in DpRVI values among several
 446 fields, even though they are in the identical phenological stage. The rate of
 447 increase in DpRVI values slows down at the end of July after the stagnation
 448 of vegetative growth and the onset of seed development. Similarly, the values
 449 of $\sigma_{VH}^0/\sigma_{VV}^0$ and RVI follow the vegetation growth trends of wheat. $\sigma_{VH}^0/\sigma_{VV}^0$
 450 increases during heading to flowering as the plant biomass increases. Similar
 451 results are also reported by Veloso et al. (2017) for cereal crops during these
 452 phenology stages.

453 The correlation analysis of vegetation indices with plant biophysical pa-
 454 rameters is shown in Fig. 14. The R^2 of DpRVI with PAI, VWC, and DB are
 455 0.62, 0.62, and 0.57, respectively, which are higher than the R^2 of $\sigma_{VH}^0/\sigma_{VV}^0$
 456 and RVI. The dispersion of DpRVI values in the correlation plot at later
 457 growth stages are likely due to scattering from the upper canopy layer (i.e.,
 458 wheat heads). Wu et al. (1985) reported similar results that the wheat heads
 459 dominate the total scattering power at the heading stage with a ground-
 460 based scatterometer experiment. However, during the ripening stage (when
 461 the heads become drier), the backscatter from the ground becomes dominant,
 462 and the backscatter power from the heads is insensitive to the moisture con-
 463 tent. Furthermore, variations in backscatter power are less prominent with
 464 changes in the leaf area or biomass (Jia et al., 2013).

465 5. Conclusion

466 We have proposed a dual-pol radar vegetation index (DpRVI) for Sentinel-
 467 1 (VV-VH) SAR data. The index is derived using the degree of polarization

468 (m) and the dominant normalized eigenvalue ($\beta = \lambda_1/\text{Span}$) obtained from
 469 the 2×2 covariance matrix. The DpRVI is assessed for three crop types (viz.,
 470 canola, soybean, and wheat) to characterize vegetation growth throughout
 471 its phenology. The DpRVI followed the advancement of plant growth until
 472 full canopy development with the accumulation of Plant Area Index (PAI)
 473 and biomass (vegetation water content (VWC) and dry biomass (DB)), which
 474 is evident from its high correlation with these parameters.

475 Among the results obtained from three different crops, canola indicated
 476 the highest correlation (R^2) with its biophysical parameters: 0.79 (PAI),
 477 0.82 (VWC), and 0.75 (DB). In contrast, DpRVI showed moderate correla-
 478 tions with biophysical parameters of wheat and soybean. It is noted that
 479 the correlations of DpRVI are comparatively better than that of $\sigma_{VH}^0/\sigma_{VV}^0$
 480 and dual-pol RVI for all crops. Instead of utilizing the polarization channel
 481 backscatter intensities, the DpRVI uses the normalized dominant eigenvalue
 482 and the degree of polarization, which are roll and polarization basis invari-
 483 ant. It can be concluded that the DpRVI effectively incorporates both the
 484 scattered and received wave information to describe the phenological changes
 485 that are vital for time-series crop monitoring.

486 Notably, the proposed DpRVI for dual-pol SAR data holds significant in-
 487 terest from an operational perspective for the Sentinel-1 Copernicus mission
 488 and upcoming SAR missions, e.g., the RADARSAT Constellation Mission
 489 (RCM) and NISAR which provide data in larger spatial extent with a short
 490 revisit time. For example, end-users might be interested in weekly vegeta-
 491 tion condition products from an operational mission like the Sentinel-1. In
 492 fact, the frequent revisit of SAR satellites is necessary to monitor critical

phenological stages during the crop season. With the synergy of Sentinel-1A and 1B, monitoring crop conditions over national scales with dual-pol indices would be an adequate proxy. However, implications with the HH-HV mode is required to be further examined as crop response could be different for horizontally polarized transmitted wave than the vertical. Moreover, experimental validation of vegetation indices on the incidence angle variations is necessary for wide swath products. The vegetation index needs to be further investigated for different cropping systems at various test sites for validation with dense time-series data cube under the JECAM SAR Inter-Comparison Experiment at an operational scale.

Appendix A. Relationship between m and β

The eigen-decomposition of a 2×2 covariance matrix, \mathbf{C}_2 can be expressed as,

$$\mathbf{C}_2 = \mathbf{U}_2 \mathbf{\Sigma} \mathbf{U}_2^{-1} \quad (\text{A.1})$$

where,

$$\mathbf{\Sigma} = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} \quad (\text{A.2})$$

is a 2×2 diagonal matrix with nonnegative elements, $\lambda_1 \geq \lambda_2 \geq 0$, which are the eigenvalues of the covariance matrix, and \mathbf{U}_2 is a 2×2 unitary matrix whose columns are the eigenvectors of the covariance matrix.

The degree of polarization (m) of the EM wave is derived from the ex-

pression given by Barakat (1977) as,

$$m = \sqrt{1 - \frac{4|\mathbf{C}_2|}{(\text{Tr}(\mathbf{C}_2))^2}} \quad (\text{A.3})$$

It can be noted that m can also be expressed in terms of the eigenvalues as,

$$m = \sqrt{\left[1 - \frac{4\lambda_1\lambda_2}{(\lambda_1 + \lambda_2)^2}\right]} = \sqrt{\left[\frac{(\lambda_1 + \lambda_2)^2 - 4\lambda_1\lambda_2}{(\lambda_1 + \lambda_2)^2}\right]} = \frac{\lambda_1 - \lambda_2}{\lambda_1 + \lambda_2} \quad (\text{A.4})$$

507 The normalized dominant eigenvalue, β is given as, $\lambda_1/\text{Span} = \lambda_1/(\lambda_1 + \lambda_2)$.
 508 Hence, the differential variation between m and β is expressed as, $\beta - m =$
 509 $\lambda_2/(\lambda_1 + \lambda_2) = \lambda_2/\text{Span}$.

510 Disclosures

511 No potential conflict of interest is reported by the authors.

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 519 cloud computing platform".

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